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Sub: Linear Algebra [Paper – XIV] (MCQ)

Practice Questions Paper

Q) Select the correct alternative for each of the following:

1) The number of vectors in any basis of a vector space V is called ----- of V .

- i) Rank ii) Nullity iii) order iv) dimension

2) If $\dim(V) = m$, $\dim(W) = n$ then $\dim(V, W) = \text{-----}$

- i) m ii) n iii) $m n$ iv) $m + n$

3) Inner product space over real field is called -----.

- i) null space ii) subspace iii) Euclidean space iv) Unitary space.

4) If $T: V \rightarrow W$ is a linear transformation and if $\dim V = 10$, $\dim \text{kernel } T = 6$ then $\dim \text{range } T = \text{-----}$

- i) 4 ii) 6 iii) 10 iv) 5

5) If $A = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$ then the characteristic polynomial of A is

- i) $x^2 + 1$ ii) $x^2 - 1$ iii) $x^2 + x$ iv) $x^2 + 2x + 1$

6) If S is an Orthonormal set then for $\alpha \in S \dots$

- i) $\|\alpha\| > 2$ ii) $\|\alpha\| = 0$ iii) $\|\alpha\| < 1$ iv) $\|\alpha\| = 1$

7) The norm of vector $u = (4, -3, 0, 1)$ is -----.

- i) 30 ii) $\sqrt{30}$ iii) 26 iv) $\sqrt{26}$

8) A non-zero vector is always -----

- i) Linearly independent ii) linearly dependent
iii) Both i) and ii) iv) All of these.

9) Which of the following is not vector space ?

- i) $R(R)$ ii) $C(C)$ iii) $R(C)$ iv) $C(R)$

10) Let $V(F)$ be a vector space, $\alpha, \beta \in F$ and $x, y \in V$. Then which of the following is incorrect?

ii) $(\alpha + \beta)(x+y) = (\alpha - \beta)(x - y)$

iv) $\alpha(-x) = -(\alpha x) = (-\alpha) x$

11) If S is set of linear independent vector then

ii) 0 may or may not be in S

iv) none of these

12) If V is vector space over field F , then the elements of F are called -----.

ii) vectors

iv) numerical constants

13) The norm of v is -----

ii) $\| \mathbf{v} \|$

iii) non-negative real number iv) All of these

14) If $A = \begin{vmatrix} 0 & i \\ i & 0 \end{vmatrix}$ then characteristic polynomial of A is -----.

iv) $(x-1)^2$

15) Finite dimensional vector space are isomorphic if and only if they have -----.

i) different dimensions ii) zero dimensions

iii) same dimensions iv) none of these.

16) Let $\lambda = 4$ is eigen value of invertible operator T then eigen value of T^{-1} is -----

iv) -2

17) If $T: V \rightarrow W$ and $S: W \rightarrow U$ are two linear transformations such that ST is one-one then

ii) T is one-one

iv) T is onto.

18) The norm of vector $u = (1, -3, 5)$ is

i) $\sqrt{35}$

ii) 35

iii) $\sqrt{34}$

iv) $\sqrt{30}$

19) A zero vector is always

i) Linearly Dependent

ii) Linearly Independent

iii) Both (i) and (ii)

iv) none of these

20) If $T: V \rightarrow W$ is a linear transformation and if $\dim V = 8$, $\text{Rank } T = 5$ then nullity $T = \dots\dots$

i) 3

ii) 8

ii) 5

iv) 1

21) If $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$ then the characteristic polynomial of A is

i) $(x+1)^2$

ii) $(x-1)^2$

iii) $(x-2)^2$

iv) $(x+2)^2$

22) If S is an Orthonormal set then for $\alpha \in S$,

i) $\|\alpha\| = 1$

ii) $\|\alpha\| = 0$

iii) $\|\alpha\| < 1$

iv) $\|\alpha\| > 2$

23) If $\dim V = n$ and $S = \{v_1, v_2, \dots, v_n\}$ spans V then S is

i) Basis of V

ii) subspace of V

iii) not basis of V

iv) none of these

24) if V and W are vector spaces over the field F then $\text{Hom}(V, W)$ is called dual space of V over F, If

i) $V = F$

ii) $W = F$

iii) $V = W$

iv) $V \neq W$

25) A zero vector is always

i) Linearly Independent

ii) Linearly Dependent

iii) Both (i) & (ii)

iv) None of these

26) If $T: V \rightarrow W$ is a linear transformation and if $\dim V = 28$ and $\dim \text{Range } T = 20$ then $\dim \text{Ker } T = \dots$

- i) 8 ii) 6 iii) 9 iv) 10

27) A linear transformation $T: V \rightarrow W$ is said to be non-singular if

- i) $\text{Ker } T = \{0\}$ ii) T is one-one
iii) T is Invertible iv) All Of these

28) V is linearly independent iff

- i) $V=0$ ii) $V \neq 0$ iii) $V=W$ iv) $V \neq W$
29) $\dim (M_{m \times n}(F)) = \dots$

- i) mn ii) m iii) n iv) None of these

30) Inner product space over complex field is called -----.

- i] Null space ii] Euclidean space iii] Unitary space iv] Subspace

31) The sum of two subspaces is -----.

- i] a group ii] a field iii] a ring iv] Subspace

32) Let $T: U \rightarrow V$ be homomorphism then kernel of T is -----.

- i] Subspace of V ii] Subspace of U iii] Quotient space of X iv] $\{0\}$

33) In the vector space $V(F)$ the scalar multiplication $(\alpha f)(x)$ for all $x \in V(F)$, $\alpha \in F$ is given by -----.

- i] $\alpha f(x)$ ii] $\alpha + f(x)$ iii] $\alpha - f(x)$ iv] $\alpha + x$

34) A non empty subset W of a vector space $V(F)$ is subspace of V If

- A] $\alpha x \in W$ B] $\alpha x + \beta y \in W$
C] $\alpha x \cdot \beta y \in W$ D] none of them

35] Let $T: V \rightarrow U$ be a homomorphism then $\ker T = \{ 0 \}$

- A] T is one one
- B] T is onto
- C] T is one one and onto
- D] None of them

36] If $S = \{ V_1, V_2, \dots, V_n \}$ is basis of V then every element of V can be expressed as a linear combination of

- A] V_1, V_2, \dots, V_{n+1}
- B] V_1, V_2, \dots, V_n
- C] linear dependent vectors
- D] None of them

37] Any two basis of finite dimensional vector space of V have -----

- A] finite number of elements
- B] same number of elements
- C] infinite number of elements
- D] none of them

38] Finite dimensional vector space V has dimension n i f f

- A] n is maximum no of L.I.
- B] n is maximum no of L.D elements
- C] n is zero elements of L.I
- D] None of them

39] If V is finite dim. vector space , $\{ V_1, V_2, \dots, V_r \}$ is a L.I subset of V then

- A] r is max.no L.I elements
- B] it can be extended to form basis
- C] it can not be extended to form basis
- D] none of them

40] Two finite dimensional vector space over F are isomorphic iff they have

- A] finite dimension
- B] disjoint dimension
- C] Same l.D elements
- D] same dimension

41] Let S be orthogonal set of non zero vectors in an inner product space V then

A] S is L.I set

B] S is L.D set

C] S is empty set

D] none of them