

***PRACTICE***

***TEST***

***PAPER***

1. Let  $f: A \rightarrow B$  and  $X \subseteq A, Y \subseteq A$  then which of the following is wrong ?

- A)  $f(X \cup Y) = f(X) \cup f(Y)$
- B)  $f(X \cap Y) = f(X) \cap f(Y)$
- C)  $f^{-1}(X \cup Y) = f^{-1}(X) \cup f^{-1}(Y)$
- D)  $f^{-1}(X \cap Y) = f^{-1}(X) \cap f^{-1}(Y)$

2. Which of the following statements is wrong ?

- A) Countable union of countable sets is countable
- B) The set of all rational numbers is countable
- C) The set of all rational numbers in the interval  $[0, 1]$  is countable
- ☒ D) The set  $\mathbb{Q} \times \mathbb{Q}$  is not countable

3. The statement "If  $A$  is any nonempty subset of set of real numbers that is bounded above, then  $A$  has a least upper bound" is well known as

- A) greatest lower bound axiom
- ☒ B) least upper bound axiom
- C) continuum axiom
- D) none of the above

4. The Cantor set  $K$  is

- A) countably finite
- B) countably infinite
- ☒ C) not countable
- D) none of the above

5. The l.u.b of the set  $\left\{1, \frac{1}{2}, \frac{1}{3}, \dots\right\}$  is

- A) 1
- B) 0
- ☒ C) does not exist
- D) none of the above

6. Every monotone decreasing sequence of real numbers is

- ☒ A) bounded above
- B) bounded below
- C) neither bounded above nor below
- D) bounded

7. Let  $A$  be a bounded set, then which of the following is always true ?
- both l.u.b and g.l.b belongs to  $A$
  - neither g.l.b nor l.u.b belongs to  $A$
  - either l.u.b or g.l.b belongs to  $A$
  - exactly one of (A), (B) and (C) holds
8. Let  $s_n = (-1)^n$  ( $n \in \mathbb{I}$ ) then  $\limsup_{n \rightarrow \infty} S_n = \dots$
- 0
  - 1
  - 1
  - does not exist
9. If  $\{S_n\}_{n=1}^{\infty}$  is a sequence of real numbers that is not bounded above, then  $\limsup_{n \rightarrow \infty} S_n = \dots$
- 0
  - 1
  - infinity
  - minus infinity
10. The limit inferior of the sequence 1, 2, 3, 1, 2, 3, ..... is
- 1
  - 2
  - 3
  - 0
11. Which of the following is true ?
- $\{(-1)^n\}_{n=1}^{\infty}$  is  $(C, 1)$  summable and  $\{n\}_{n=1}^{\infty}$  is not  $(C, 1)$  summable
  - $\{(-1)^n\}_{n=1}^{\infty}$  is  $(C, 1)$  not summable but  $\{n\}_{n=1}^{\infty}$   $(C, 1)$  summable
  - neither  $\{(-1)^n\}_{n=1}^{\infty}$  is  $(C, 1)$  summable nor  $\{n\}_{n=1}^{\infty}$   $(C, 1)$  summable
  - both  $\{(-1)^n\}_{n=1}^{\infty}$  and  $\{n\}_{n=1}^{\infty}$  are  $(C, 1)$  summable
12. Let  $\{a_n\}_{n=1}^{\infty}$  be a non decreasing sequence of positive terms then which of the following is not true ?
- $\sum_{n=0}^{\infty} 2^n a_{2^n}$  converges implies  $\sum_{n=1}^{\infty} a_n$  converges
  - $\sum_{n=0}^{\infty} 2^n a_{2^n}$  diverges implies  $\sum_{n=1}^{\infty} a_n$  diverges
  - $\sum_{n=0}^{\infty} 2^n a_{2^n}$  diverges need not imply  $\sum_{n=1}^{\infty} a_n$  diverges
  - $\sum_{n=0}^{\infty} a_n$  converges implies  $\lim_{n \rightarrow \infty} n a_n = 0$



13. The series  $1 - 1 + \frac{1}{2} - \frac{1}{2} + \frac{1}{3} - \frac{1}{3} + \dots$  is

- A) convergent
- B) divergent
- C) oscillatory
- D) none of (A), (B) or (C)

14. Let  $f(x) = x$  ( $0 \leq x \leq 1$ ). Let  $\sigma = \left\{0, \frac{1}{4}, \frac{2}{4}, \frac{3}{4}, 1\right\}$  be a division of  $[0, 1]$  then

$U[f; \sigma] = \dots$

- A)  $\frac{3}{8}$
- B)  $\frac{5}{8}$
- C) 0
- D)  $\frac{1}{2}$

15. The function  $f(x) = \frac{\sin x}{x}$  ( $x \neq 0$ ) and  $f(0) = 1$  is

- A) Not Riemann integrable in  $[0, 1]$
- B) Riemann integrable in  $[0, 1]$
- C) Not Riemann integrable in  $[1, 2]$
- D) Not Riemann integrable in any interval  $[a, b]$

16. Let  $f(x)$  be defined in  $[0, 1]$  as follows

$f(x) = 1$  when  $x$  is rational and

$f(x) = 0$  when  $x$  is irrational

Then the upper integral of  $f$  over  $[0, 1]$  is

- A) 1
- B) 0
- C)  $\frac{1}{2}$
- D)  $\frac{1}{3}$

17. The improper integral  $\int_0^1 \frac{\sin x}{x^2}$  is

- A) convergent
- B) divergent
- C) neither convergent nor divergent
- D) none of (A), (B) or (C)

18. Which one of the following statements is not true ?

- A) Every convergent sequence is Cauchy
- B) Every Cauchy sequence is convergent
- C) A convergent sequence has a unique limit
- D) If a Cauchy sequence has a convergent subsequence, then the whole sequence is convergent

19. In  $\mathbb{R}^1$  the sequence  $\left\{\frac{1}{n}\right\}_{n=1}^{\infty}$  is

- A) convergent but not Cauchy
- B) not convergent but Cauchy
- C) convergent Cauchy sequence
- D) neither convergent nor Cauchy

20. Which one of the following statements is not true ?

- A) Every Cauchy sequence is bounded
- B) Every bounded sequence is Cauchy
- C) Every monotone non decreasing sequence which is bounded above is convergent
- D) The discrete metric space  $\mathbb{R}_d$  is complete

21. Which one of the following statements is not true ?

- A) The metric space  $\ell^2$  is complete
- B) A metric space is compact if it is totally bounded and complete
- C) A metric space is compact iff it has Heine-Borel property
- D) A finite metric space need not be compact

22. The closure of  $(0, 1) \subset \mathbb{R}^1$  is

- A)  $(0, 1]$
- B)  $[0, 1)$
- C)  $(0, 1)$
- D)  $[0, 1]$

23. Let  $f: M_1 \rightarrow M_2$  be a continuous function, then which of the following is false

- A)  $f(A)$  is open whenever  $A \subset M_1$  is open
- B)  $f^{-1}(A)$  is open whenever  $A \subset M_2$  is open
- C)  $f^{-1}(A)$  is closed whenever  $A \subset M_2$  is closed
- D)  $f(A)$  is connected whenever  $A \subset M_1$  is connected

24. Which one of the following is false ?

- A) closed subset of compact space is compact
- B) compact subset of a metric space is closed
- C) continuous image of compact metric space is compact
- D) the metric space  $\mathbb{R}^1$  is compact

25. Which one of the following is false ?

- A) A continuous function on a closed bounded interval in  $\mathbb{R}^1$  is bounded
- B) The set  $(0,1) \subset \mathbb{R}^1$  is compact
- C) The metric space  $\mathbb{R}^2$  is complete
- D) A continuous function on a compact metric space is always uniformly continuous

26. The function  $f(x) = x^2$ ,  $x \in \mathbb{R}^1$  is

- A) uniformly continuous on  $\mathbb{R}^1$
- B) continuous but not uniformly continuous on  $\mathbb{R}^1$
- C) not continuous on  $\mathbb{R}^1$
- D) uniformly continuous but not continuous on  $\mathbb{R}^1$

27. Let  $M$  be a metric space with the property " $M$  has no non-empty proper subset which is both open and closed". then  $M$  is

- A) compact
- B) dense
- C) connected
- D) not connected

28. The function  $f(z) = |z|^2$  is

- A) analytic at origin
- B) differentiable at origin
- C) not differentiable at origin
- D) not continuous at origin

29. Let  $f(z) = u + iv$  be a complex valued function of complex variable  $z = x + iy$ , the

equations  $\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y}$ ,  $\frac{\partial v}{\partial x} = -\frac{\partial u}{\partial y}$  are called

- A) Laplace equations
- B) Gauss' equations
- C) Cauchy Riemann equations
- D) None of the above



30. For a complex variable  $z$ , Taylor expansion for  $e^z$  is

A)  $1 + \frac{z}{1!} + \frac{z^2}{2!} + \dots$

B)  $1 - \frac{z}{1!} + \frac{z^2}{2!} - \dots$

C)  $\frac{z}{1!} + \frac{z^2}{2!} + \dots$

D)  $\frac{z}{1!} - \frac{z^3}{3!} + \frac{z^5}{5!} - \dots$

✓31. The set  $\{z : |z - 1| + |z - 5| = 10\}$  represents

A) a circle

B) ellipse

C) hyperbola

D) parabola

✓32. The equation of a circle with center at  $a$  and radius  $r$  is

A)  $z = a + r$

B)  $|z - r| = |a|$

C)  $|z - a| = r$

D)  $(z - a)^n = r^n$

✓33. The equation  $|z - 1| = |z - 3|$  represents

A) the line  $x - y = 2$

B) the circle  $x^2 + y^2 = 4$

C) the line  $x = 2$

D) the line  $y = 2$

✓34. The points represented by  $z_1, z_2, z_3, z_4$  lie on a circle if and only if their  $c$  ratio is

A) purely imaginary

B) real

C) zero

D) 1

✓35. Let  $\arg \left( \frac{z - z_1}{z - z_2} \right) = 4$ , then  $z$  lies on a

A) circle

B) ellipse

C) hyperbola

D) parabola

36. The Taylor expansion of  $\frac{1}{1-z}$  ( $|z| < 1$ ) is

A)  $\frac{z}{1!} + \frac{z^2}{2!} + \dots$

B)  $1 + \frac{z}{1!} + \frac{z^2}{2!} + \dots$

C)  $1 + z + z^2 + \dots$

D)  $1 - z + z^2 - \dots$

✓37. Let  $\omega = (\cos \theta + i \sin \theta)$  then  $\omega^5 =$

A)  $\cos^5 \theta + i \sin^5 \theta$

B)  $\cos \theta + i \sin \theta$

C)  $\cos 5\theta + i \sin 5\theta$

D)  $\cos^5 \theta - i \sin^5 \theta$

38. Let  $x + \frac{1}{x} = 2$ , then  $x^n + \frac{1}{x^n} =$  \_\_\_\_\_

- A) 2  
B) n  
C) 2n  
D)  $2^n$

39. The value of the integral  $\int_{|z|=1} \frac{dz}{z}$  is

- A)  $2\pi$   
B)  $2\pi i$   
C) 0  
D) 1

40. The value of the integral  $\int_{|z|=1} \frac{zdz}{(z-1)^2}$  is

- A)  $2\pi$   
B)  $2\pi i$   
C) 0  
D) 1

41. The function  $f(z) = \bar{z}$  is

- A) analytic everywhere  
B) differentiable everywhere  
C) nowhere differentiable  
D) nowhere continuous

42. Let  $z_1, z_2$  be complex numbers then  $\arg(z_1 z_2) =$  \_\_\_\_\_

- A)  $\arg(z_1) \arg(z_2)$   
B)  $\arg(z_1) + \arg(z_2)$   
C)  $\arg(z_1) - \arg(z_2)$   
D)  $\arg(z_1) / \arg(z_2)$

43. A nonempty subset H of a group  $(G, \cdot)$  is a subgroup of G if and only if  $a, b \in H$  implies

- A)  $a + b \in H$   
B)  $(a \cdot b)^{-1} \in H$   
C)  $a \cdot b^{-1} \in H$   
D)  $a \cdot b \in H$

44. Intersection of two subgroups of a group

- A) is a subgroup  
B) need not be a subgroup  
C) is always empty  
D) contains only one element

45. Let H be a subgroup of G. For  $a, b \in G$ , we say that a is congruent to b mod H if

- A) a divides b  
B) b divides a  
C)  $a \cdot b \in H$   
D)  $a \cdot b^{-1} \in H$



46. Let  $H$  be a subgroup of a finite group  $G$ . Then,  
 A)  $O(G)$  divides  $O(H)$   
 B)  $O(H)$  divides  $O(G)$   
 C)  $O(H) = O(G)$   
 D)  $O(H)^2$  divides  $O(G)$
47. Let  $G$  be a finite group and  $H$  be a subgroup of  $G$ . Then index of  $H$  in  $G$  is equal to  
 A) number of elements in  $H$   
 B) number of distinct right (left) cosets of  $H$   
 C) number of distinct right (left) cosets of  $G$   
 D) number of elements in  $G/H$
48. Let  $H$  and  $K$  be the two subgroups of a group  $G$ . Then  $HK$  is a subgroup of  $G$  if and only if  
 A)  $HK = H$   
 B)  $KH = K$   
 C)  $HK < KH$   
 D)  $HK = KH$
49. An infinite cyclic group has  
 A) only one generator  
 B) two generators  
 C) three generators  
 D) infinite generator
50. If  $f: G \rightarrow G'$  is a homomorphism then  $\ker f$  is  
 A) not a subgroup  
 B) abelian subgroup  
 C) normal subgroup  
 D) cyclic subgroup
51. A homomorphism  $f: G \rightarrow G'$  is one-one if and only if  
 A)  $\ker f$  is nontrivial  
 B)  $\ker f = \phi$   
 C)  $\ker f = \{e\}$   
 D)  $\ker f = G$
52. A cycle of a permutation  $f = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 4 & 2 & 3 & 5 & 1 & 6 \end{pmatrix}$  is  
 A)  $(2\ 3\ 6)$   
 B)  $(1\ 4\ 5)$   
 C)  $(1\ 2\ 3)$   
 D)  $(1\ 5\ 4)$
53. A ring  $R$  with unity is called a division ring if  
 A)  $R$  is a group w.r.t. multiplication  
 B)  $R$  is a group w.r.t. addition  
 C) Non zero elements of  $R$  is a group w.r.t. multiplication  
 D) Non zero elements of  $R$  is a group w.r.t. addition

54. The set of all even integers under addition and multiplication forms a ring
- with unity
  - without unity
  - with zero divisors
  - with multiplicative inverse
55. A ring  $R$  is called simple if
- $R$  has nontrivial ideals
  - $R$  has only trivial ideals
  - $R$  has only one nontrivial ideal
  - None of these
56. Let  $R$  be a commutative ring with unity. An ideal  $M$  of  $R$  is called maximal ideal of  $R$  if and only if
- $R/M$  is a field
  - $R/M$  is a division ring
  - $R/M$  contains divisors of zero
  - $R/M$  is a proper ideal

57. An ideal  $P$  of  $R$  is called a prime ideal if  $a \cdot b \in P$  implies
- $a \in P$  and  $b \in P$
  - $a \in P$  or  $b \in P$
  - $a \notin P$  and  $b \notin P$
  - $a$  and  $b$  are prime

58. Fourier transform of a function  $f(x)$ ,  $F\{f(x)\} =$

- $\frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{ipx} f(x) dx$
- $\frac{1}{2\pi} \int_{-\infty}^{\infty} e^{ipx} f(x) dx$
- $\frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-ipx} f(x) dx$
- $\sqrt{2\pi} \int_{-\infty}^{\infty} e^{ipx} f(x) dx$

59. The infinite Fourier sine transform of  $f(x)$ ,  $0 < x < \infty$  is defined by  $F_s\{f(x)\} =$

- $\sqrt{2\pi} \int_0^{\infty} f(x) \sin px \, dx$
- $\sqrt{\frac{2}{\pi}} \int_0^{\infty} f(x) \sin px \, dx$
- $\frac{1}{\sqrt{2\pi}} \int_0^{\infty} f(x) \sin px \, dx$
- $\sqrt{\frac{\pi}{2}} \int_0^{\infty} f(x) \sin px \, dx$

✓ 60. If  $\tilde{f}_c(p)$  is a Fourier cosine transform of  $f(x)$  then Fourier cosine transform of  $f(ax)$  is

A)  $\frac{1}{a} \tilde{f}_c(ap)$

B)  $a \tilde{f}_c(ap)$

C)  $a \tilde{f}_c\left(\frac{p}{a}\right)$

D)  $\frac{1}{a} \tilde{f}_c\left(\frac{p}{a}\right)$

✓ 61. If  $\tilde{f}(p)$  is a complex Fourier transform of  $f(x)$  then complex Fourier transform of  $f(x - a)$  is

A)  $e^{ipa} \tilde{f}(p)$

B)  $e^{ipa} \tilde{f}(p - a)$

C)  $e^{-ipa} \tilde{f}(p)$

D)  $e^{-ipa} \tilde{f}(p - a)$

✓ 62. If  $\tilde{f}_s(p)$  is Fourier sine transform of  $f(x)$  then Fourier sine transform of  $f(x) \cos ax$  is

A)  $\frac{1}{2} [\tilde{f}_s(p + a) - \tilde{f}_s(p - a)]$

B)  $\frac{1}{2} [\tilde{f}_s(p + a) + \tilde{f}_s(p - a)]$

C)  $2 [\tilde{f}_s(p + a) + \tilde{f}_s(p - a)]$

D) None of these

✓ 63. If  $\tilde{f}(p)$  is a complex Fourier transform of  $f(x)$  then complex Fourier transform of  $f'(x)$  is

A)  $ip \tilde{f}(p)$

B)  $p \tilde{f}(ip)$

C)  $-p \tilde{f}(-ip)$

D)  $-ip \tilde{f}(p)$

✓ 64. If  $F$  and  $G$  are integrable functions over  $(-\infty, \infty)$  then convolution of  $F$  and  $G$   $H(x) = F * G(x) =$

A)  $\int_{-\infty}^{\infty} F(u) G(u) du$

B)  $\int_{-\infty}^{\infty} F(u) G(x - u) du$

C)  $\int_{-\infty}^{\infty} F(x - u) G(x - u) du$

D)  $\int_{-\infty}^{\infty} F(x + u) G(u) du$



65. The kernel of the Hankel transform  $H_n\{f(x)\}$  is
- A)  $x J_n(px)$  B)  $J_n(px)$
- C)  $\frac{1}{x} J_n(px)$  D)  $xf(x)$

66. If  $\tilde{f}(p) = \int_0^\infty f(r) r J_n(pr) dr$  is the Hankel transform of the function  $f(r)$  then by inversion formula,  $f(r) =$

- A)  $\int_0^\infty \tilde{f}(p) p J_n(pr) dp$  B)  $\int_0^\infty \tilde{f}(p) r J_n(pr) dp$
- C)  $\int_0^\infty \tilde{f}(p) pr J_n(pr) dp$  D)  $\int_0^\infty \tilde{f}(p) J_n(pr) dp$

67. The Hankel transform of  $\frac{e^{-ax}}{x}$  taking  $xJ_0(px)$  as the kernel, is

- A)  $(a^2 + p^2)^{-1/2}$  B)  $(a^2 - p^2)^{-1/2}$
- C)  $(a^2 - p^2)^{3/2}$  D)  $(a^2 + p^2)^{3/2}$

68. The Hankel transform of  $\frac{e^{-x}}{x^2}$  taking  $xJ_1(px)$  as the Kernel is

- A)  $\frac{[(1+p^2)^{1/2} - 1]}{p}$  B)  $\frac{[(1+p^2)^{1/2} - 1]}{p}$
- C)  $\frac{[(1-p^2)^{-1/2} + 1]}{p}$  D)  $\frac{[(1-p^2)^{-1/2} - 1]}{p}$

69. If  $\tilde{f}(p) = \frac{e^{-ap}}{p}$ ,  $(n=0)$  then  $H^{-1}\{\tilde{f}(p)\} =$

- A)  $(a^2 + x^2)^{-1/2}$  B)  $(a^2 + x^2)$
- C)  $(a^2 - x^2)^{-1/2}$  D)  $(a^2 + x^2)^{1/2}$

70. If  $p$  is a root of the equation  $J_n(pa) = 0$  then  $H_n\left\{\frac{df}{dx}\right\} =$

A)  $\frac{p}{2n}[(n-1)H_{n-1}\{f(x)\} - (n+1)H_{n+1}\{f(x)\}]$

B)  $\frac{2p}{n}[(n-1)H_{n-1}\{f(x)\} + (n+1)H_{n+1}\{f(x)\}]$

C)  $\frac{p}{2n}[(n-1)H_{n-1}\{f(x)\} - (n+1)H_{n+1}\{f(x)\}]$

D)  $\frac{2p}{n}[(n-1)H_{n-1}\{f(x)\} + (n+1)H_{n+1}\{f(x)\}]$

71. Let  $T: U \rightarrow V$  be linear transformation and  $\dim U = \dim V$ . If  $T$  is on to then

A)  $R(T) = U$

B)  $R(T) = V$

C)  $\dim R(T) < \dim V$

D)  $N(T)$  not equal to  $\{0\}$

72. If  $T: V_2 \rightarrow V_3$  is such that  $T(1, 0) = (1, 2, 3)$ ,  $T(0, 1) = (2, 3, 1)$  and  $S: V_3 \rightarrow V_3$  is such that  $S(1, 0, 0) = (-1, 0, 1)$ ,  $S(0, 1, 0) = (0, 1, 2)$  and  $S(0, 0, 1) = (1, -1, 0)$  then  $(ST)(0, 1)$  is

A)  $(2, -1, 5)$

B)  $(-2, 1, 5)$

C)  $(2, -1, -5)$

D)  $(-1, 2, 8)$

73. Let  $T: U \rightarrow V$  and  $S: V \rightarrow W$  be two linear transformations then  $ST$  is one-one if

A)  $S$  is one-one

B)  $T$  is one-one

C)  $ST$  is onto

D)  $ST = \{0\}$

74. A linear map  $T$  is idempotent if and only if

A)  $T^{-1} = I$

B)  $T^2 = I$

C)  $T^2 = T$

D)  $T = T^{-1}$

75. If  $T: U \rightarrow V$  is linear transformation then  $\text{Rank } T + \text{Nullity } T =$

A)  $\dim U$

B)  $\dim V$

C) infinity

D)  $\dim U + \dim V$

76. The set  $\{(1, 2), (2, 4)\}$  is

A) Linearly independent

B) Linearly dependent

C) Basis of  $R^2$

D) None of these

77.  $|\langle u, v \rangle| \leq$

A)  $\|u\| \|v\|$

B)  $|u| |v|$

C)  $\|u\| + \|v\|$

D) None of these

78.  $\|u+v\|^2 + \|u-v\|^2$  is equal to

A)  $\|u\|^2 + \|v\|^2$

B)  $\|u\|^2 - \|v\|^2$

C)  $2[\|u\|^2 + \|v\|^2]$

D)  $2[\|u\|^2 - \|v\|^2]$

79. An orthogonal set of non-zero vectors in an inner product space  $V$  is

A) Linearly dependent

B) Orthogonal

C) Linearly independent

D) Zero space

80. The set  $\{(1, 1), (2, 3)\}$  is

A) Linearly dependent

B) Basis

C) Linearly independent

D) None of these

81. The least number of negative roots of the equation  $x^5 + 2x^4 - 3x^3 - 8 = 0$  is

A) 2

B) 3

C) 4

D) 5

82. The equation of sphere centered at  $C(2, 3, -4)$  and radius 4 is

A)  $x^2 + y^2 + z^2 - 4x - 6y + 8z - 13 = 0$

B)  $x^2 + y^2 + z^2 - 4x + 6y + 8z + 13 = 0$

C)  $x^2 + y^2 + z^2 - 4x - 6y + 8z + 13 = 0$

D)  $x^2 + y^2 + z^2 - 4x - 6y - 8z - 13 = 0$

83. If one of the roots of an equation is  $\alpha + i\beta$ , then its one of the other roots is

A)  $-\alpha + i\beta$

B)  $-\alpha - i\beta$

C)  $\alpha - i\beta$

D)  $\beta - i\alpha$



84. The second degree equation of sphere with center  $(u, v, -w)$  and radius  $\sqrt{u^2 + v^2 + w^2 + d}$  is

- A)  $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$   
 B)  $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz - d = 0$   
 C)  $x^2 + y^2 + z^2 - 2ux - 2vy - 2wz + d = 0$   
 D)  $x^2 + y^2 + z^2 - 2ux - 2vy - 2wz - d = 0$

85. An equation of the lowest degree with rational coefficients having  $\sqrt{5} + 2\sqrt{6}$  as one of its roots, is

- A)  $x^4 + 10x^2 - 1 = 0$   
 B)  $x^4 - 10x^2 + 1 = 0$   
 C)  $x^4 - 10x^2 - 1 = 0$   
 D)  $x^4 + 10x^2 + 1 = 0$

86. The expansion of  $\cos x$  is

- A)  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots$   
 B)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$   
 C)  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$   
 D) none of these

87. Let  $f(D)y = 0$  be the linear differential equation with constant coefficients. If the auxiliary equation of this equation has the roots 2 and 3 then its complete solution is given by

- A)  $y = Ae^{3x} + Be^{2x}$   
 B)  $y = Ae^{-3x} + Be^{-2x}$   
 C)  $y = Ae^{-3x} + Be^{2x}$   
 D)  $y = Ae^{3x} + Be^{-2x}$

where A and B are constant.

88.  $1 - x + x^2 - x^3 + \dots$  ( $x \neq 1$ ) is the expansion of

- A)  $\frac{1}{1+x}$   
 B)  $\frac{1}{1-x}$   
 C)  $e^x$   
 D)  $\log x$

89. Let  $f(D)y = 0$  be the linear differential equation with constant coefficients. If the auxiliary equation of this equation has the roots  $\pm i$  then its complete solution is given by

- A)  $y = e^x (A \cos x + B \sin x)$   
 B)  $y = e^{ix} (A \cos(x) + B \sin(x))$   
 C)  $y = A \cos(x) + B \sin(x)$   
 D)  $y = A \cos ix + B \sin ix$

where A and B are constant

90. The distance between two points  $\left(4, \frac{4\pi}{6}\right)$  and  $\left(2, \frac{\pi}{6}\right)$  is given by
- A)  $-2\sqrt{5}$  B) 20  
C)  $\sqrt{5}$  D)  $2\sqrt{5}$
91. The function  $f(x, y)$  with  $A = f_{xx}(a, b)$ ,  $B = f_{xy}(a, b)$  and  $C = f_{yy}(a, b)$  has an extreme value at  $(a, b)$  if
- A)  $AC - B^2 > 0$  B)  $AC - B^2 < 0$   
C)  $AB - C^2 > 0$  D)  $AB - C^2 < 0$
92. The Geometric series  $\sum_{n=0}^{\infty} \left(\frac{1}{3}\right)^n$
- A) is convergent B) diverges to  $\infty$   
C) diverges to  $-\infty$  D) oscillates
93. The value of the  $\lim_{x \rightarrow \infty} x \sin \frac{1}{x}$  is equal to
- A) -1 B) 0  
C) 1 D) none of these
94. The value of  $\beta(1, 2) =$
- A)  $\frac{1}{2}$  B)  $\frac{1}{4}$   
C) 2 D) 3
95. Which one of the following is not an indeterminate form ?
- A)  $\infty + \infty$  B)  $\infty - \infty$   
C)  $\infty / \infty$  D)  $1^0$
96. One of the solutions of the differential equation  $\frac{d^2y}{dx^2} + P \frac{dy}{dx} + Qy = R$  is  $e^{-x}$  if
- A)  $1 - P - Q = 0$   
B)  $1 + P - Q = 0$   
C)  $1 + P + Q = 0$   
D)  $1 - P + Q = 0$

97. The Laplace Transform of  $\frac{\sin t}{t}$  is  $\tan^{-1}\left(\frac{1}{s}\right)$  then Laplace transform of  $\frac{\sin at}{t}$  is

A)  $\tan^{-1}\left(\frac{a}{s}\right)$

B)  $\tan^{-1}\left(\frac{s}{a}\right)$

C)  $\tan^{-1}(as)$

D)  $\tan^{-1}\left(\frac{1}{as}\right)$

98. Solution of the differential equation  $yz \log z dx - zx \log z dy + xy dz = 0$  is

A)  $e^{x \log z} = cy$

B)  $x + y + z = c$

C)  $x \log z = cy$

D) None of these

99. The solution of partial differential equation  $(D^2 - 7DD' + 12D'^2)z = 0$  is

A)  $z = \phi_1(y - 3x) + \phi_2(y - 4x)$

B)  $z = \phi_1(y + 3x) + \phi_2(y - 4x)$

C)  $z = \phi_1(y - 3x) + \phi_2(y + 4x)$

D)  $z = \phi_1(y + 3x) + \phi_2(y + 4x)$

100. The infinite series  $\sum \frac{1}{n^{3/2}}$  is

A) convergent

B) divergent

C) oscillates

D) none of these